

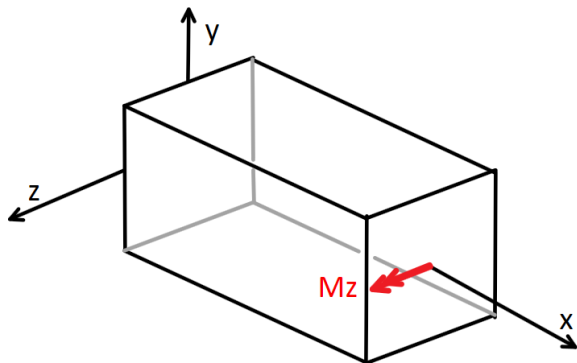
MAE 343. Intermediate Mechanics

Stress IV : 2-plane Bending, Other Sections

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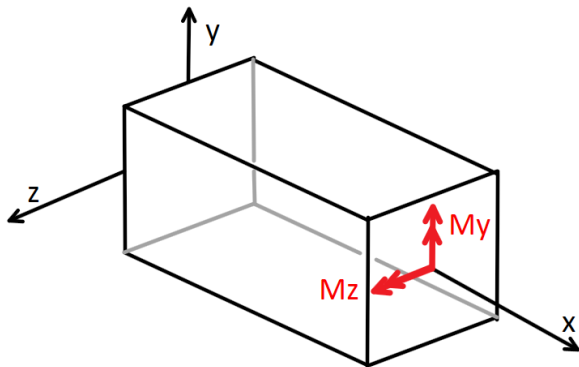
Review: bending on a single plane



$$\sigma_x = \frac{-y M_z}{I_z}$$

Single plane bending, bending on the xy plane.

2-plane bending formula

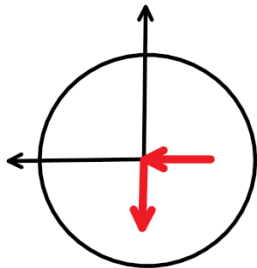


$$\sigma_x = -\frac{y M_z}{I_z} + \frac{z M_y}{I_y}$$

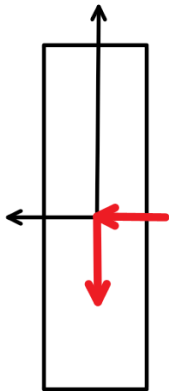
Add bending on the xz plane, with moment M_y .



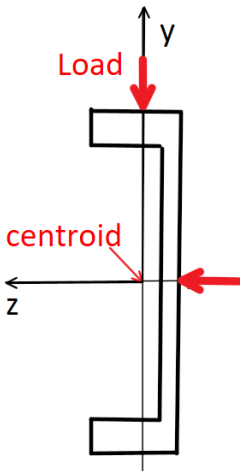
2-plane bending formula, applicability



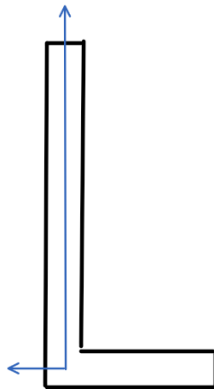
Circular



Doubly
symmetric

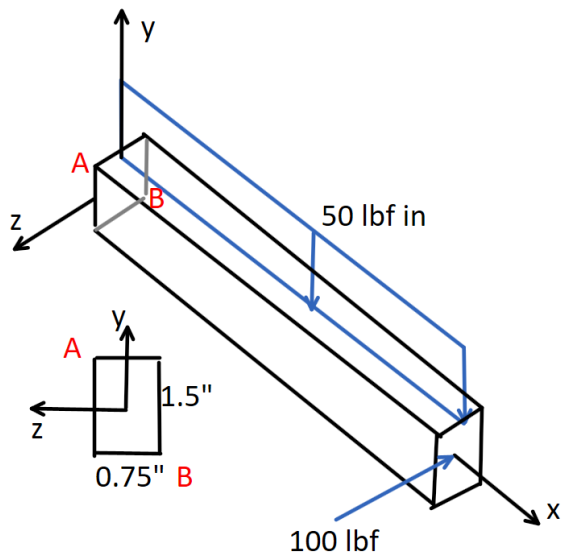


Symmetric
w.r.t. z



Not
symmetric

Example 3-6



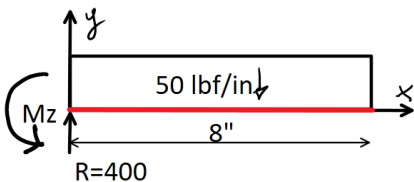
$$I_z = \frac{0.75 \times 1.5^3}{12} = 0.2109 \text{ in}^4$$

$$I_y = \frac{1.5 \times 0.75^3}{12} = 0.05273 \text{ in}^4$$

$$\text{At A: } y = 1.5/2 = 0.75'' \quad ; \quad z = 0.75/2 = 0.375''$$

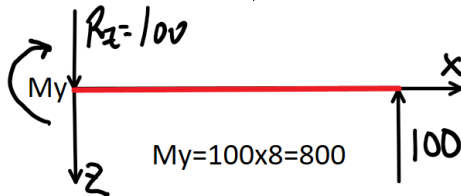
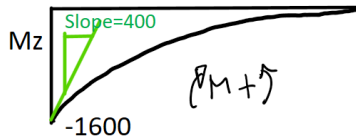
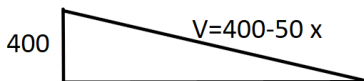
$$\text{At B: } y = -0.75'' \quad ; \quad z = -0.375''$$

Example 3-6, 2/5

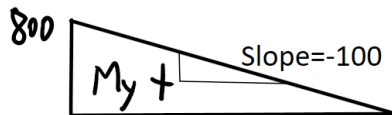
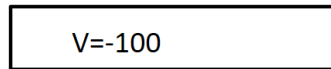


$$R = 50 \times 8 = 400$$

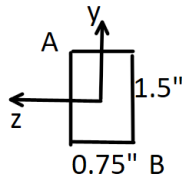
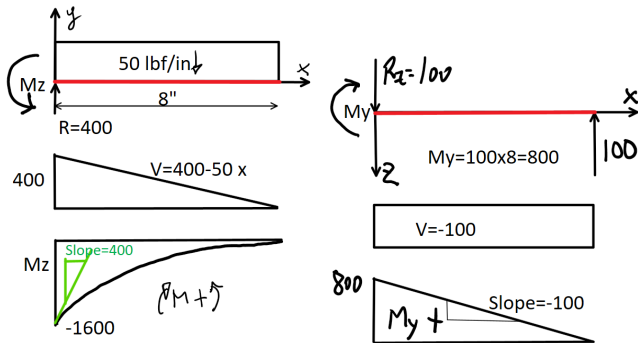
$$M = 400 \times 4 = 1600$$



$$M_y = 100 \times 8 = 800$$



Example 3-6, point A

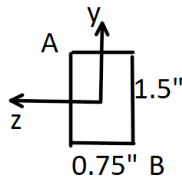
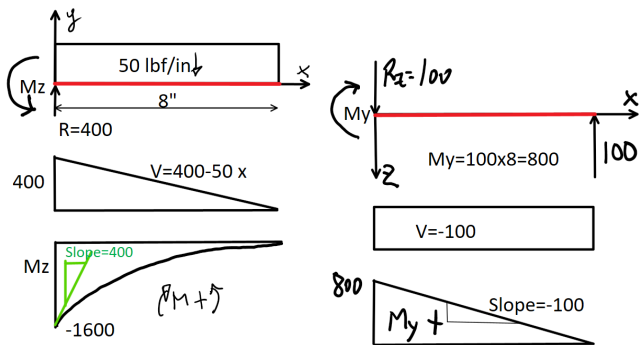


$$\sigma_x = -\frac{M_z y}{I_z} + \frac{M_y z}{I_y}$$

$$\sigma_x^A = -\frac{-1600 \times 0.75}{0.2109} + \frac{800 \times 0.375}{0.05273}$$

$$\sigma_x^A = 11380 \text{ psi}$$

Example 3-6, point B



$$\sigma_x = -\frac{M_z y}{I_z} + \frac{M_y z}{I_y}$$

$$\sigma_x^B = -\frac{-1600 \times -0.75}{0.2109} + \frac{800 \times -0.375}{0.05273}$$

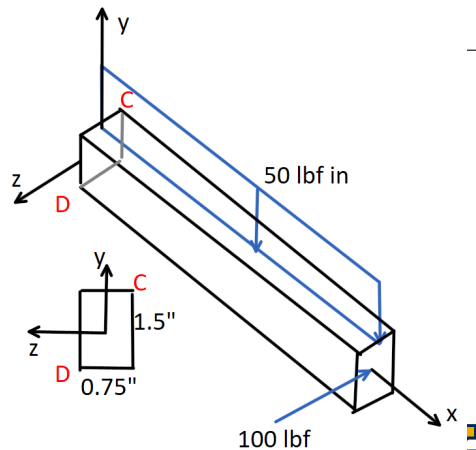
$$\sigma_x^B = -11380 \text{ psi}$$

Example 3-6, at the remaining corners

$$\sigma_x = -\frac{M_z y}{I_z} + \frac{M_y z}{I_y}$$

$$\sigma_x^C = -\frac{-1600 \times 0.75}{0.2109} + \frac{800 \times -0.375}{0.05273} = 0$$

$$\sigma_x^D = -\frac{-1600 \times -0.75}{0.2109} + \frac{800 \times 0.375}{0.05273} = 0$$



Summary

- With at least one axis of symmetry, the 2-term formula is applicable
- Just do 2 sets of diagrams, one for the xy-plane and another for xz-plane
- Must check all corners to find out which one has the largest stress



Thank you!

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