

# MAE 343. Intermediate Mechanics

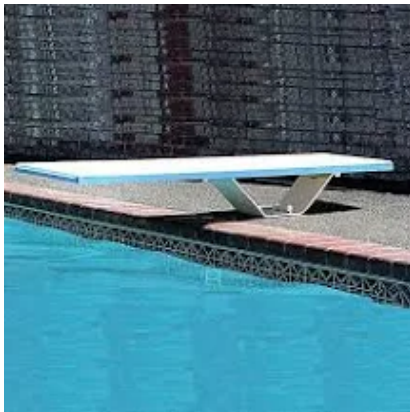
## Chapter 3: Mechanics Beam Diagrams

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## Example 1: Diving Board



## Example 1: Diving Board, cont'd

Draw the V and M diagrams. Add eqns.

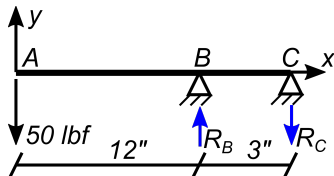
$$\sum F_y = 0 : -50 + R_B - R_C = 0$$

$$\sum M_c = 0: \text{cancel unknown at C}$$

$$50 \times 15 - R_B \times 3 = 0 :$$

$$R_B = 50 \times 15 / 3 = 250 \text{ lbf}$$

$$\text{From 1st eq. } R_C = R_B - 50 = 200 \text{ lbf}$$



## Example 1: Diving Board, cont'd

$$R_B = 250 \text{ lbf}$$

$$R_C = 200 \text{ lbf}$$

Using shear convention, draw the V-diagram.

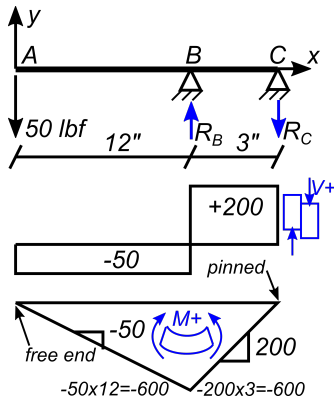
Draw the M-diagram using the fundamental

eqn.  $V = dM/dx$ , or  $M = \int_0^x V dx$

Add eqns. to the diagrams:

$$0 < x < 12 : M = -50x$$

$$12 < x < 15 : M = -600 + 200(x - 12)$$



## Example 2: Simply Supported Beam

Draw the V and M diagrams. Add eqns.

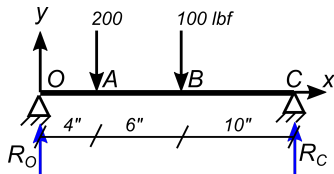
$$\sum F_y = 0 : R_O + R_C = 300$$

$$\sum M_O = 0: \text{cancel unknown at O}$$

$$20R_C - 200 \times 4 - 100 \times 10 = 0:$$

$$R_C = (800 + 1000)/20 = 90 \text{ lbf}$$

$$\text{From 1st eq. } R_O = 300 - 90 = 210 \text{ lbf}$$



## Example 2: Simply Supported Beam, cont'd

Draw the V and M diagrams. Add eqns.

$$R_C = 90 \text{ lbf}$$

$$R_O = 210 \text{ lbf}$$

Using shear convention, draw the V-diagram.

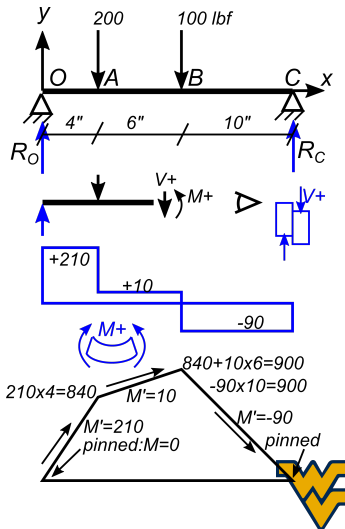
Draw the M-diagram using the fundamental

eqn.  $V = dM/dx$ , or  $M = \int_0^x V dx$

$$0 < x < 4 : M = 210x$$

$$4 < x < 10 : M = 840 + 10(x - 4)$$

$$10 < x < 20 : M = 900 - 90(x - 10)$$



## Example 3: Concentrated Moment

Draw the V and M diagrams. Add eqns.

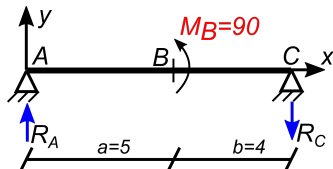
$$R_A = R_C$$

$\sum M_A = 0$ : cancel unknown at A

$$R_C(a + b) - M_B = 0$$

$$R_C = 90 / (5 + 4) = 10$$

From 1st eq.  $R_A = 10$  lbf



## Example 3: Concentrated Moment

Draw the V and M diagrams. Add eqns.

$$R_C = 10 \text{ lbf}$$

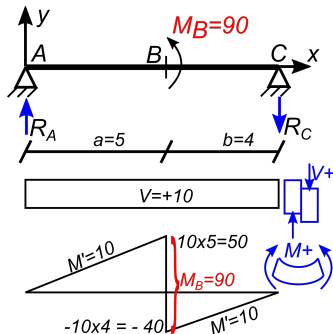
$$R_A = 10 \text{ lbf}$$

Using shear convention, draw the V-diagram.

Draw the M-diagram using the fundamental eqn.  $V = dM/dx$ , or  $M = \int_0^x V dx$

$$0 < x < 5 : M = 10x$$

$$5 < x < 9 : M = -40 + 10(x - 5)$$





# Summary and Conclusions

- ▶ First, calculate the reactions.
- ▶ From the reactions, you get the shear diagram.
- ▶ From the shear diagram, you get the bending moment diagram.
- ▶ Homework is on WebWork
- ▶ Next lecture: Morh's circle 2D
- ▶ THANK YOU

